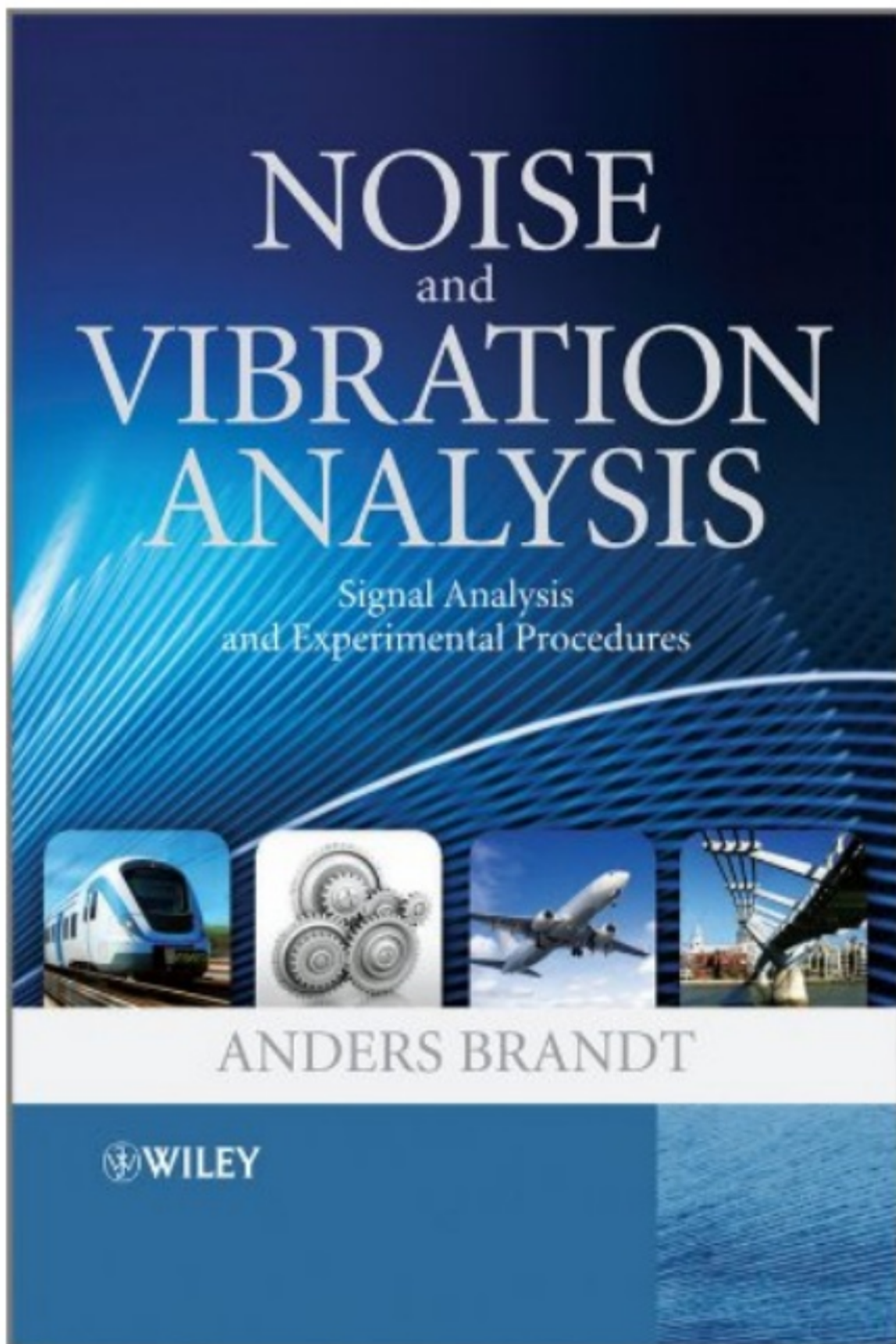


**Noise and Vibration Analysis: Signal Analysis and
Experimental Procedures by Anders Brandt**



NOISE AND VIBRATION ANALYSIS

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NOISE AND VIBRATION ANALYSIS

SIGNAL ANALYSIS AND EXPERIMENTAL PROCEDURES

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